

Research Article

Detection of Breast Cancer in Infrared Thermographies Using Stochastic Techniques in a FPGA Platform

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Abstract

Thermo graphical infrared images to predict the existence of a thermal anomaly according to symmetry in breasts by using stochastic methods and fuzzy logic control is proposed. Statistical results are established through entropy, kurtosis and media to evaluate symmetry grade between the right and left breast. To predict the grade of breast cancer associated to the tissue and take a decision a fuzzy controller is designed in base to symmetric assessments distribution. The proposed method is implemented on a FPGA platform optimizing hardware requirements and improves response time. Results show that the error of the prediction method can be an alternative to detect cancer if the image source are far away from the critical errors, interference to the source or infrared image processed.

Keywords: Infrared images; FPGA; Stochastic methods; Fuzzy controller breast cancer

1. Introduction

Currently there are several methods to detect cancer, which can detect its appearance and more likely to treat it successfully. Detection methods most commonly used today require complex machines that do not give a result to

the naked eye, but these need to be analyzed by a specialist. These methods are invasive and need machines too expensive. Also, a thermo graphical record of an individual's body can be created and processed for further analysis to determine the existence of a thermal anomaly. Also, image segmentation involves the use of various techniques to extract and separate relevant information from an image. [1-7]. Stochastic techniques can be used for detection thermal anomalies, more precisely thermal asymmetry in the chest area to detect cancer. In the other hand, novel fuzzy control methods have been developed and implemented as a programming platform to control different processes in different areas. Due to their heuristic nature associated with simplicity and effectiveness for both linear and non-linear systems, fuzzy logic controllers (FLC) has showed their outstanding features in implementations for solar tracking systems, mechatronics systems, etc. [8-13].

The main aim of this paper is to use stochastic techniques and fuzzy logic controller to detect the thermal asymmetry in the region in a simple and precise way in comparison to the already existing techniques of breast cancer detection. The structure of rest of the paper is as follow. Section 2, describe the stochastic processes of the termographical images in order to elaborate a stochastic approach for detecting the breast cancer. In Section 3, based on the stochastic approach, the grade of breast cancer is determined according to a fuzzy control as alternative to manage the stochastic information. Section 4, shows the characterization of this propose by simulation and experimental results. The paper concludes with Section 4, where conclusions are drawn.

2. Stochastic techniques for detection thermal asymmetries

Figure 1, represents in a modular way the processes to be performed for the breast cancer detection based on thermographic images. The first block refers to a thermal image obtained by a device outside the system which is a thermographic camera. Once the thermographic image is obtained, it is processed by a conversion to grayscale taking the luminance of the pixels, a segmentation to separate the background of the image and the information that correspond to the chest on which the study will be performed. Then, since the body symmetry must be identified, the main image is divided in two sub-images. These sub-images contain only the tissue corresponding to the left and right chest. Next, stochastic techniques are applied to each breast to determine the asymmetry grade between these two images without considering the size of the samples. Finally, Linguistic variables are proposed to design the fuzzy control to determine the grade of breast cancer associated to the tissue.

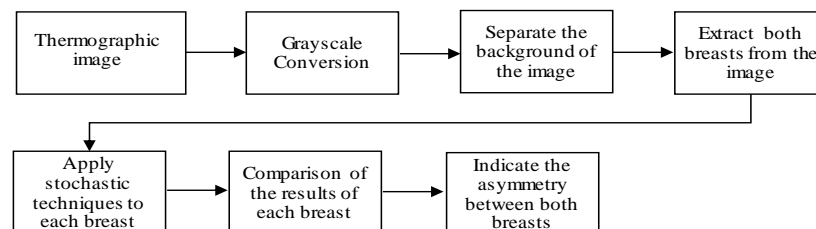


Figure1: Schematic diagram proposed to detect breast cancer using stochastic techniques.

2.1 Grayscale conversion

To convert the grayscale image, first it is separated into three spectra information RGB. Once the image is separated, it is converted to gray scale and processed to normalize the image values. This consists in establishing a minimum reference pixel value which will be used to represent different temperatures in the human tissue. Eliminating background noise in the image, it is segmented in order to isolate both breast tissues and find some key points within the image which are able to provide where begins and ends in the thermal image. Figure 2, shows the key points locations represented by: Top Right Point (TRP), Left Upper Point (LUP), Right Lower Point (RLP), Left Lower Point (LLP). The first point (TRP), is find through locating the first pixel not belonging to the bottom of the image, starting with the top left of the image, using:

$$TRP = \sum_{(1,1)}^{(\frac{X}{2},1)} p_{(X,Y)} = 0 \quad (1)$$

Where X represents the total width of the image and determines the beginning of the body in the image and Y, represents the total height of the image measured from top to bottom.

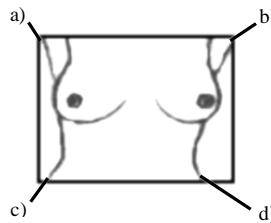


Figure 2. Key points locations in the image. a) TRP, b) LUP, c) RLP, d) LLP.

In similar way is found the second point (LUP), only that the counting starts from the pixel (1, X), which would be the top row and the final column of the image. Third point (RLP), start with the first pixel at the left bottom (Y, 1). It starts counting the number of zeros that are in this row from left to right until it reaches $X / 2$, which is the half of the image, using:

$$RLP = \sum_{(1,Y)}^{(\frac{X}{2},Y)} p_{(X,Y)} = 0 \quad (2)$$

Finally the fourth point (LLP), represent the first pixel corresponding to the left side of the body in the thermal image. It consists in counting the pixels belonging to the bottom of the image or zero value, starting from the lower left (X, Y), using:

$$LLP = \sum_{(X,Y)}^{(\frac{X}{2},Y)} p_{(X,Y)} = 0 \quad (3)$$

Once the four main points of the image are found, lines are drawn to joins the points TRP with LLP and LUP with RLP, as is shown in Figure 3. The intersection of both points will be called the geometric center (GC). To obtain this point, is necessary to determine the angles shown in Figure 4.

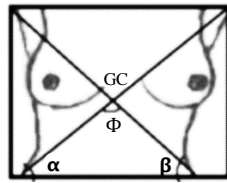


Figure 3

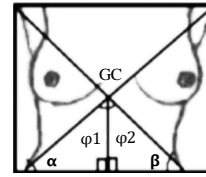


Figure 4

The angle of the line joining the points LUP and RLP is called α . To determine the value of this angle, the distance between these points on the horizontal axis X is obtained, using:

$$x_1 = X - RLP - LUP \quad (4)$$

Then, angle α is calculated by:

$$\alpha = \tan^{-1} \left(\frac{Y}{x_1} \right) \text{ o } \alpha = \tan^{-1} \left(\frac{Y}{(X - RLP - LUP)} \right) \quad (5)$$

Same manner, angle called β , corresponding to the line joining the points TRP and LLP is obtained by:

$$x_2 = X - LLP - TRP \quad (6)$$

$$\beta = \tan^{-1} \left(\frac{Y}{x_2} \right) \text{ o } \beta = \tan^{-1} \left(\frac{Y}{(X - LLP - TRP)} \right) \quad (7)$$

Third angle φ , is obtained by:

$$\varphi = 180 - \alpha - \beta \quad (8)$$

Considering the angles β and φ in addition to the distance from RLP to LLP, which forms the total base of the triangle, the distance from RLP to GC called DC, is found by:

$$DC = \frac{(X - RLP - LLP)}{\sin \varphi} * \sin \beta \quad (9)$$

Distance from LLP to GC called LC, is found through the α and φ angles and the distance from RLP to LLP, by:

$$LC = \frac{(X - PID - PII)}{\sin \varphi} * \sin \alpha \quad (10)$$

Once the distance DC and LC have been obtained, the height of the GC point called GCY is obtained by:

$$GCY = Y - DC * \sin \alpha \quad (11)$$

Horizontal distance of the GC, called GCX is determined by:

$$GCX = RLP + (DC * \cos \alpha) \quad (12)$$

Once these points are located, the image of the breast is separate in two, right and left.

2.2. Stochastic process

Stochastic techniques are applied to the regions of interest to detect thermal asymmetry in base to the pixel values between right and left breasts. Arithmetic mean, is the first function to know thermal asymmetries which, is known as the mean sample [14, 15, 16], given by:

$$\bar{X} = \frac{\sum_{i=1}^n X_i}{n} \quad (13)$$

This value corresponds to the middle of all pixels values in a range from 0 to 255, which correspond to the maximum admissible thermal value. The mean value must be the same for both breasts. In case of an asymmetry or

anomaly, mean value differs. Another function to consider, is the deviation of the pixels from the mean value called variance, given by:

$$S^2 = \frac{\sum (X_i - \bar{X})^2}{(n-1)} \quad (14)$$

Where S^2 is the variance, $\sum (X_i - \bar{X})^2$ is the sum of the variances for each pixel, n number of total pixels.

If the variance moves to the left (being smaller) indicates that the asymmetry is below of the average temperature, in the other case, (being greater) would indicate that the temperature is above the average. This is relevant to determine a possible cancerous tissue in anyone breast. Another function is the kurtosis which allow to know how the pixels values are concentrated in the standard central distribution area. Kurtosis coefficient is obtained by:

$$g_2 = \frac{\frac{1}{n} \sum (X_i - \bar{X})^4 * n_i}{\left(\frac{1}{n} \sum (X_i - \bar{X})^2 * n_i\right)^2} - 3 \quad (15)$$

Where g_2 is the kurtosis coefficient, X_i is the value of each pixel, \bar{X} is the mean and n_i is the frequency at which the pixel appears.

Finally, entropy is one of the most used function for detection thermal asymmetries. When temperature distribution in both breasts is similar, the entropy value tends to be the same, and is given by:

$$\text{Entropy} = - \sum_{i=0}^{L-1} \text{Prob}(\log_2(\text{Prob})) \quad (16)$$

Where Prob, corresponds to the probability that a certain pixel value will appear in the image, which is represented

$$\text{as } \frac{\text{Pix}}{m*n} [17].$$

2.3 Fuzzy Control

The fuzzy control structure, is designed to reduce the computational complexity, since the operations performed in each stage like multiplications, sum, divider, power, etc, are not made using hardware but look-up tables. The look-up tables play a crucial role in all stages of a Mamdani fuzzy control, and thereby, the operations tend to be very few. It is deriving from the principle of memory that the look-up tables serve to storing the membership values represented in this study by 8 bits which generate 256-levels in a binary data. Figure. 5, shows the block diagram of the Fuzzy control proposed. It consists of two inputs and one output. To convert the rigid input values to fuzzy values, data from the ADC converter act as a memory addressing while membership values are stored in look-up tables. For each rigid input value corresponding one membership value. These membership values are the input to the inference stage where they are processed through the Mamdani max-min implication, having as a result, the conclusion of the fuzzy rules. In the aggregation stage, the conclusion of each rule is combined and summed to obtain a final conclusion. Then, defuzzification stage converts the membership values to a rigid value. Finally, it is converted to a voltage using a DAC. All stages are implemented in a FPGA platform using description language VHDL code. The Output of the Fuzzy control will be the Cancer diagnosis.

2.4 Fuzzification

Input variables are defined based on the difference in the Media (DM) and Kurtosis (DK) values between the left and right breast. Each variable is represented by five fuzzy sets which conform to the linguistic variables. The fuzzy sets for the DM variable are labeled as VL (Very light), S (Small), R (Regular), L (large) and VH (Very large). The fuzzy sets for the DK variable are the same labels. The output fuzzy variable is called a cancer diagnosis (CD), and also, is represented by five fuzzy sets labeled as H (healthy), C (caution), M (minimal), D (drastic) and VD (very drastic). Each variable has a universe of discourse in the digital domain in the range from 0 to 1023, which is proposed using 10 bits of resolution. Figure. 6, shows the fuzzy sets proposed in the universe of discourse for the inputs and output variables. For the membership values, 8 bits of resolution are used, which divides the membership values in a range from 0 to 255 values, which is adequate because the range is from 0 to 1. So, each fuzzy set contain 256 levels. The base of each fuzzy set is found for those levels whose membership value is zero. This values are especially useful because they allow to know if the value of the rigid input signal belongs to a given fuzzy set.

2.5 Inference

For the inference and aggregation stages, Mamdani method is used through the max-min operations. For this, an inference matrix is generated to place the output inference values using rules If...Then by making a correlation between the membership values obtained in the fuzzification stage, using:

$$\mu_{A \rightarrow B}(x, y) = \min[\mu_A(x), \mu_B(y)] \quad (17)$$

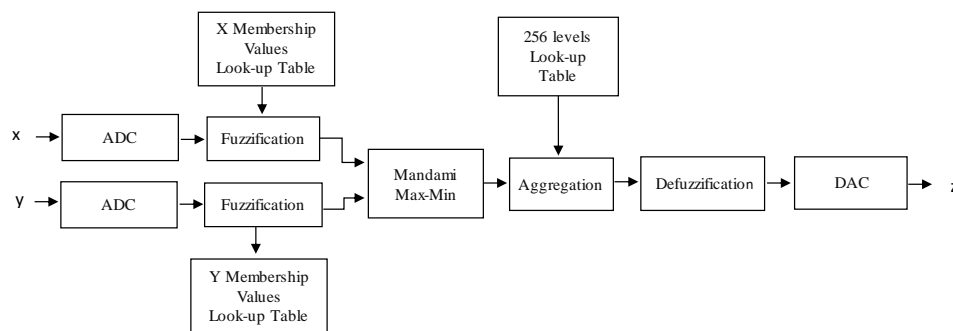


Figure 5: Block diagram of the FLC proposed.

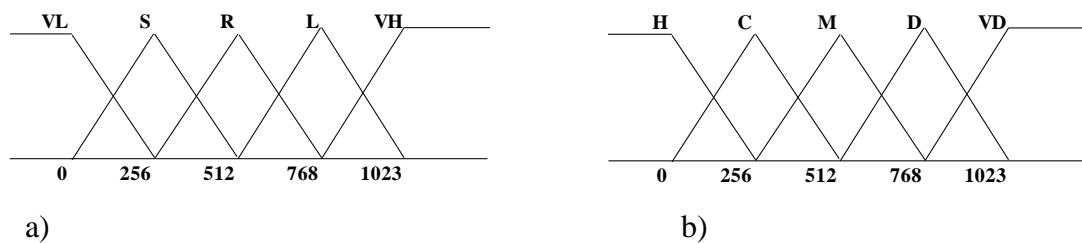


Figure 6: Membership functions for a) inputs and b) output variables.

This way, the matrix will have 25 possible output values obtained from the evaluation of the rules shown in Table I. It involves a comparison between two membership values reached in each rule and selecting the minimum membership value.

The aggregation stage is carried out by the method of maximum membership value obtained in the inference stage whose value is different to 0, given by:

$$\mu_{B^l}(y) = \max \left[\mu_{F_1^l}(x_1), \dots, \mu_{F_n^l}(x_n) \right] \quad (18)$$

It is the union of the activated rules for each column in the matrix. In this case, five columns. It takes into account those rules that have a nonzero value. For this case, all values contained in a column are compared and selecting the maximum value and so on. These membership values fall in the universe of discourse of the output fuzzy sets call Diagnosis cancer, which are used for the defuzzification stage. This stage converts a fuzzy value to a real value.

Table 1: Inference matrix.

ln 1 \ ln 2	nA	nB	nC	nD	nE
mA	min_00	min_01	min_02	min_03	min_04
mB	min_10	min_11	min_12	min_13	min_14
mC	min_20	min_21	min_22	min_23	min_24
mD	min_30	min_31	min_32	min_33	min_34
mE	min_40	min_41	min_42	min_43	min_44

3.3 Defuzzification

In order to save processing time and hardware on the FPGA, defuzzification with 256-levels are used to obtain the rigid output value from the aggregation vector, given by:

$$DC_{\text{Def}} = \sum_{i=0}^{\alpha_{\text{max}}} \frac{\frac{x_f^{\alpha_i} - x_0^{\alpha_i}}{2} + x_0^{\alpha_i}}{N} \quad (19)$$

Where DC_{Def} is the diagnosis cancer, N , is the number of fuzzy set activated in the aggregated vector, $x_f^{\alpha_i}$ is the final point of the level where membership value reached in the aggregated vector, $x_0^{\alpha_i}$ is the initial point of the same level. The schematic design in VHDL for the FLC implemented is shown in Figure 7, which consist of fuzzification, inference (min), aggregation (max) and defuzzification stages.

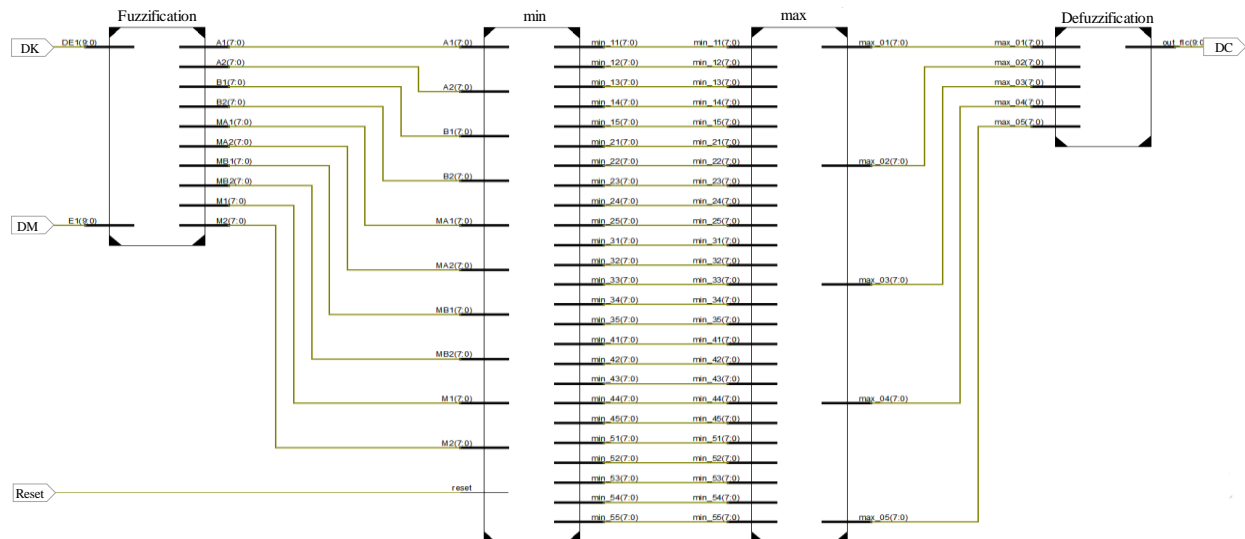


Figure 7: Schematic design for the FLC implemented.

3. Experimental Results

Measurement results were carried out taking into account a database belonging to the Visual Lab DMR (Database for Mastology Research), which is an online platform that stores mastological images for the breast cancer by your research group. Registration results of this group were compared with this proposal. To determine if the thermographs correspond to a group of healthy or cancer, a series of minimum and maximum values for the difference of Mean, Kurtosis and Entropy were taken. Also, and according to the method used by Visual Lab, the following was taking into account:

- To determine a normal thermal asymmetry, difference between average Media values belonging to the right and left breasts can have a maximum value of 3.
- Pixels distribution around the average value for each breast must be similar for both breasts. The difference between these values must not be greater than 0.63 to be considered as a normal asymmetry.
- Difference between the entropy values can be until 0.284, to determine a normal thermal asymmetry.

This manner, for diagnosing cancer, tests were performed on 44 of 72 thermographies. Tests were carried out connecting two probes to the FLC inputs through ADC cables in a digital domain according to results presented in Table II, which corresponding to the difference between Media and Kurtosis, (only 20 tests values are presented). The internal clock signal to synchronize the FLC process implemented from advanced VHDL synthesis was establish at 500 KHz. The implementation can be used for five or more linguistic variables, but can be easily expanded repeating sections of code, also can be used for any type of fuzzy set. This manner, the FLC determine thermal asymmetry between both breasts, diagnosing the grade of cancer. The experimental results were compared in a theoretical way with the method obtained by the Matlab Fuzzy Logic ToolBox. For example, considering the values of test 2, whose values are DE= 2.3199 and DK= 1.8546 introduced as inputs x and y. The digital output

from the FPGA board was CAUTION whose digital value is 319, corresponding to the caution set, whereas in MatLab Fuzzy Logic ToolBox, the digital value was 333. As can be seen, the FLC implemented on the FPGA provides very approximate values to those obtained by the Matlab Fuzzy Logic ToolBox. Then, each simulation and experimental result was evaluated with respect to the Visual Lab researchers result, which was classified as healthy or cancer presented in Table III in the column named Status and in FLC/FPGA column our results. Result differs from the expert group, perhaps because the values, not represent a specific temperature since the colors are not linked to the temperatures, since these are relative to the maximum and minimum temperature of the object being photographed. As can be seen, results obtained here (with a relatively large slot of tests), fall into the healthy case where the values for the input signals representing the difference of Media and Kurtosis. This manner, 23 tests of 44, are similar to the Visual Lab group whose diagnosis were healthy, 2 were cancerous, whereas 8 were Caution, 9 were Medium and 2 were Drastic which differ from the Visual Lab group whose diagnosis were healthy. One therefore would expect little change in the diagnosis under different pixels' distribution of the image due to its luminance parameter. Also, there would likewise be little variation in the image when some interferences are considered. Even though the results obtained cannot be ignored since difference is not greater than 15%, which tells us that the system proposed has around 85% accuracy. Finally, the mean square error (MSE) is obtained applying (20), to the data values of Table II. The MSE is 1.75%, which is very acceptable considering that this method uses iterations and 8 bits for sample.

$$MSE = \sqrt{\frac{\sum_{i=0}^N (FLC/FPGA - MATLAB)^2}{N}} \quad (20)$$

Table 2: Theoretical stochastic values.

Test		Right breast	left breast	Difference	Test		Right breast	Left breast	Difference
2	Mean	189.9702	192.2901	2.3199	110	Mean	162.6852	179.435	16.7498
	Kurtosis	9.9634	11.823	1.8596		Kurtosis	-0.0734	2.4391	2.5125
	Entropy	6.1376	6.1924	0.0548		Entropy	6.4431	6.476	0.0329
4	Mean	157.3825	160.5498	3.1673	137	Mean	154.7768	157.2495	2.4727
	Kurtosis	0.3616	0.6211	0.2595		Kurtosis	0.9232	1.5119	0.5887
	Entropy	7.0687	6.9596	0.1091		Entropy	6.5786	6.6505	0.0719
6	Mean	197.2744	190.2085	7.0659	151	Mean	167.6576	158.0755	9.5821
	Kurtosis	9.3388	6.9071	2.3317		Kurtosis	3.4973	1.8772	1.6201
	Entropy	6.1191	5.9903	0.1288		Entropy	6.4522	6.4549	0.0027
32	Mean	171.8384	180.9627	9.1243	180	Mean	128.6276	150.3287	21.7011
	Kurtosis	2.7953	3.4158	0.6205		Kurtosis	1.5523	-0.3771	1.9294
	Entropy	6.8115	6.6782	0.1333		Entropy	6.7056	7.1278	0.4222

36	Mean	152.2936	162.8829	10.5893	199	Mean	150.4432	159.5188	9.0756
	Kurtosis	1.0196	1.4089	0.3893		Kurtosis	1.8215	3.5167	1.6952
	Entropy	6.7617	6.771	0.0093		Entropy	6.5804	6.3796	0.2008
48	Mean	179.0939	179.5077	0.4138	213	Mean	165.0241	174.6383	9.6142
	Kurtosis	3.8035	3.3025	0.501		Kurtosis	0.1204	1.073	0.9526
	Entropy	6.3846	6.5698	0.1852		Entropy	6.8433	6.6365	0.2068
52	Mean	180.1167	179.6209	0.4958	217	Mean	149.0823	150.5191	1.4368
	Kurtosis	4.3003	3.1966	1.1037		Kurtosis	0.5826	0.3408	0.2418
	Entropy	6.4258	6.7089	0.2831		Entropy	6.8168	6.9688	0.152
57	Mean	159.6835	160.185	0.5015	266	Mean	180.34	162.9223	17.4177
	Kurtosis	0.8558	0.3802	0.4756		Kurtosis	4.1713	1.6453	2.526
	Entropy	6.8391	6.9607	0.1216		Entropy	6.5858	6.964	0.3782
70	Mean	155.8591	164.8692	9.0101	267	Mean	177.6323	175.3411	2.2912
	Kurtosis	2.0115	3.8171	1.8056		Kurtosis	4.9955	4.8096	0.1859
	Entropy	6.5067	6.5266	0.0199		Entropy	6.4502	6.4638	0.0136
106	Mean	134.1366	141.9478	7.8112	274	Mean	174.4745	179.1222	4.6477
	Kurtosis	1.1034	1.603	0.4996		Kurtosis	2.0989	3.6991	1.6002
	Entropy	6.7237	6.6675	0.0562		Entropy	6.762	6.7353	0.0267

Table 3: Comparison between medical (VisualLab) results and those obtained in Matlab and FLC/FPGA.

Test	VisualLab	Matlab	FLC/FPGA	Fuzzy Set
2	Healthy	333	319	Caution
4	Healthy	128	127	Healthy
6	Healthy	538	511	Medium
15	Healthy	179	203	Healthy
16	Healthy	538	511	Medium
20	Healthy	128	127	Healthy
24	Healthy	128	127	Healthy
26	Healthy	538	511	Medium
31	Healthy	333	319	Healthy
32	Healthy	333	319	Healthy
36	Healthy	333	319	Healthy
48	Healthy	128	127	Healthy

52	Healthy	128	127	Caution
57	Healthy	128	127	Healthy
62	Healthy	128	127	Healthy
65	Healthy	742	703	Drastic
66	Healthy	128	127	Healthy
70	Healthy	538	511	Medium
91	Healthy	128	127	Healthy
93	Healthy	371	395	Caution
97	Healthy	333	319	Caution
99	Healthy	128	127	Healthy
104	Healthy	333	319	Caution
105	Healthy	128	127	Healthy
106	Healthy	329	311	Caution
110	Healthy	742	703	Drastic
132	Healthy	437	415	Medium
135	Healthy	538	511	Medium
137	Healthy	128	127	Healthy
145	Healthy	128	127	Healthy
147	Healthy	128	127	Healthy
151	Healthy	436	415	Medium
152	Healthy	333	319	Caution
155	Healthy	128	127	Healthy
161	Healthy	128	127	Healthy
163	Healthy	128	127	Healthy
168	Healthy	128	127	Healthy
169	Healthy	210	223	Healthy
174	Healthy	333	319	Caution
180	Cancer	775	799	Drastic
181	Cancer	333	319	Caution
188	Healthy	128	127	Healthy
189	Healthy	538	511	Medium
190	Healthy	538	511	Medium

Conclusions

This paper compares and experimentally confirm breast cancer detection through the modeling, simulation, and measurement using stochastic techniques in a FPGA platform. Stochastic equations were developed for analysis of infrared images, and a fuzzy logic control was designed and implemented to illustrate the relationship to the stochastic results for detection cancer. The fuzzy controller provides very approximate values to detect at multiple grades or in a universe of discourse, different grades of cancer. Results are provided in which simulations and measurement show stable performance in the processes and in the must cases are according to the Visual Lab group diagnosing. The technique has a high percentage of accuracy in terms of cancer detection.

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